Examining the Use of the LOCUS Assessment with Undergraduate Students

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### Statistics Education Instruments

- **Conceptual Understanding**: Levels of Conceptual Understanding in Statistics (LOCUS; Jacobbe et al., 2014; Whitaker et al., 2015)
  - 4 components: Formulate Questions, Collect Data, Analyze Data, and Interpret Results
  - Designed for grades 9-12, desire to use in undergraduate courses
- Attitudes: Survey of Attitudes Towards Statistics (SATS; Schau, 1992, 2003)
  - 4 components (SATS-28): Affect, Value, Difficulty, and Cognitive Competence
  - 6 components (SATS-36): *Interest* and *Effort* with the SATS-28 component
  - Widely used in undergraduate courses (Ramirez et al., 2012)

### Goals & Data

- 1. Examine the factor structure of the LOCUS when used with undergraduate students
  - Pairwise-complete observations (N = 963) were used
- 2. Model the relationship between attitudes (as measured by the SATS) and conceptual understanding in statistics (as measured by the LOCUS) using logistic regression
  - Pairwise-complete data: pre (N=328) and post (N=291)
    - LOCUS attempts that were less than 5 minutes removed



We thank Dr. Alana Unfried of California State University, Monterey Bay for providing the data used in the analysis.

### Goal 1: Explore Factor Structure of LOCUS

- A four-factor solution was of interest to investigate the proposed fourconstruct structure
- The scree plots below suggested also trying a two-factor solution
- We decided to find two-factor and four-factor solutions, both pre and post

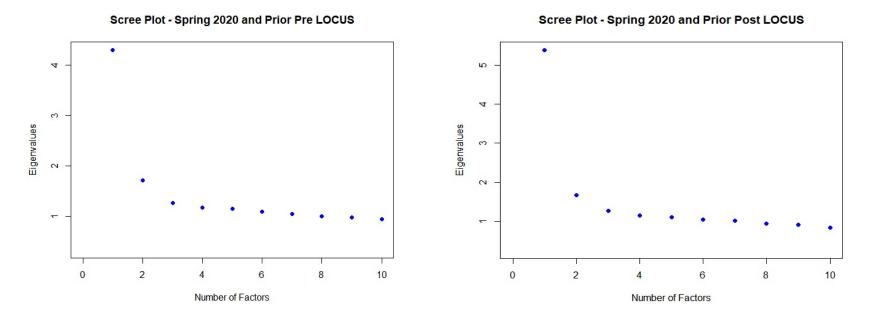


Table of loadings for four-factor solution of posttest with varimax rotation

|         | Factor 1 | Factor 2 | Factor 3 | Factor 4 | Communality | Nominal Construct   |
|---------|----------|----------|----------|----------|-------------|---------------------|
| Item 2  | 0.7478   | 0.1660   | 0.0421   | 0.0450   | 0.5906      | Formulate Questions |
| Item 5  | 0.3018   | 0.1629   | 0.0219   | -0.2212  | 0.1670      | Formulate Questions |
| Item 9  | 0.4820   | 0.4235   | 0.2006   | 0.0464   | 0.4541      | Formulate Questions |
| Item 12 | 0.2293   | 0.3318   | 0.2781   | 0.2005   | 0.2802      | Formulate Questions |
| Item 3  | 0.6124   | 0.1920   | 0.0083   | 0.0583   | 0.4154      | Collect Data        |
| Item 6  | 0.3202   | 0.1976   | 0.1113   | -0.0773  | 0.1599      | Collect Data        |
| Item 10 | 0.3594   | 0.2014   | 0.1305   | -0.0569  | 0.1900      | Collect Data        |
| Item 13 | 0.3175   | 0.4343   | 0.1444   | -0.0644  | 0.3144      | Collect Data        |
| Item 21 | 0.0979   | 0.3778   | -0.1314  | 0.2129   | 0.2149      | Collect Data        |
| Item 7  | 0.3518   | 0.2712   | 0.1155   | 0.0460   | 0.2128      | Analyze Data        |
| Item 11 | 0.2224   | 0.2762   | 0.3274   | 0.1720   | 0.2625      | Analyze Data        |
| Item 15 | 0.2796   | 0.0419   | 0.1687   | 0.0229   | 0.1089      | Analyze Data        |
| Item 16 | 0.1272   | 0.1090   | 0.3743   | -0.0755  | 0.1738      | Analyze Data        |
| Item 18 | 0.0927   | -0.0748  | 0.4415   | 0.0554   | 0.2122      | Analyze Data        |
| Item 20 | 0.1235   | 0.1924   | 0.3767   | 0.0916   | 0.2025      | Analyze Data        |
| Item 1  | 0.6085   | 0.1840   | 0.2388   | 0.0455   | 0.4633      | Interpret Results   |
| Item 4  | 0.5156   | 0.1695   | 0.2739   | 0.1815   | 0.4025      | Interpret Results   |
| Item 8  | 0.5318   | 0.1484   | 0.3680   | -0.0573  | 0.4436      | Interpret Results   |
| Item 14 | 0.2383   | -0.0655  | 0.2579   | 0.0575   | 0.1309      | Interpret Results   |
| Item 17 | 0.0097   | -0.0289  | 0.3509   | -0.1005  | 0.1342      | Interpret Results   |
| Item 19 | 0.0908   | 0.0687   | 0.3914   | 0.0038   | 0.1662      | Interpret Results   |
| Item 22 | 0.3702   | 0.8852   | 0.0103   | -0.1199  | 0.9351      | Interpret Results   |
| Item 23 | 0.0138   | 0.0460   | -0.0022  | 0.4671   | 0.2205      | Interpret Results   |
|         |          |          |          |          |             |                     |

We considered an item as loaded onto (or sufficiently associated with) a factor if the absolute value of its loading on that factor was greater than 0.4, as suggested by Swisher et al. (2004). If an item loads onto a factor, it is highlighted under that factor.

Proportion of

Variance 0.1332 0.0816 0.0619 0.0213 Explained

Cumulative Variance 0.1332 0.2149 0.2768 0.2981 Explained

### Table of loadings for two-factor solution of posttest with varimax rotation

|                                     | Factor 1 | Factor 2 | Communality | Nominal Construct   |
|-------------------------------------|----------|----------|-------------|---------------------|
| Item 2                              | 0.6307   | 0.2197   | 0.4461      | Formulate Questions |
| Item 5                              | 0.3217   | 0.0505   | 0.1060      | Formulate Questions |
| Item 9                              | 0.6488   | 0.2061   | 0.4634      | Formulate Questions |
| Item 12                             | 0.3928   | 0.2397   | 0.2118      | Formulate Questions |
| Item 3                              | 0.5634   | 0.1470   | 0.3391      | Collect Data        |
| Item 6                              | 0.3672   | 0.1321   | 0.1523      | Collect Data        |
| Item 10                             | 0.3973   | 0.1628   | 0.1844      | Collect Data        |
| Item 13                             | 0.5319   | 0.0985   | 0.2926      | Collect Data        |
| Item 21                             | 0.3385   | -0.1650  | 0.1418      | Collect Data        |
| Item 7                              | 0.4466   | 0.1344   | 0.2175      | Analyze Data        |
| Item 11                             | 0.3508   | 0.2904   | 0.2074      | Analyze Data        |
| Item 15                             | 0.2241   | 0.2287   | 0.1025      | Analyze Data        |
| Item 16                             | 0.1509   | 0.3483   | 0.1441      | Analyze Data        |
| Item 18                             | -0.0055  | 0.4676   | 0.2186      | Analyze Data        |
| Item 20                             | 0.2172   | 0.3253   | 0.1530      | Analyze Data        |
| Item 1                              | 0.5575   | 0.3492   | 0.4327      | Interpret Results   |
| Item 4                              | 0.4824   | 0.3675   | 0.3678      | Interpret Results   |
| Item 8                              | 0.4702   | 0.4515   | 0.4249      | Interpret Results   |
| Item 14                             | 0.1131   | 0.3347   | 0.1248      | Interpret Results   |
| Item 17                             | -0.0263  | 0.3200   | 0.1031      | Interpret Results   |
| Item 19                             | 0.0990   | 0.3684   | 0.1455      | Interpret Results   |
| Item 22                             | 0.8137   | -0.0563  | 0.6653      | Interpret Results   |
| Item 23                             | 0.0512   | 0.0229   | 0.0031      | Interpret Results   |
|                                     |          |          |             |                     |
| Proportion of<br>Variance Explained | 0.1730   | 0.0725   |             |                     |
| Cumulative<br>Variance Explained    | 0.1730   | 0.2456   |             |                     |

Variance Explained

We considered an item as loaded onto (or sufficiently associated with) a factor if the absolute value of its loading on that factor was greater than 0.4, as suggested by Swisher et al. (2004). If an item loads onto a factor, it is highlighted under that factor.

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## Goal 1: Explore Factor Structure of LOCUS

- A clean factor solution aligned with the hypothesized model was not found when using the post-course data
- Two-factor and four-factor solutions were found, but neither result in item groupings that are meaningful
- More work is needed!
- For future analyses, a single LOCUS composite score will be used

# Goal 2: Model Attitudes and Conceptual Understanding

- Ramirez et al. (2012) suggest that attitudes towards statistics play a critically important role in one's learning of the subject
- Long standing interest in the relationship between attitudes and achievement
- We will model the relationship between SATS scale scores (predictors) and LOCUS score (response)
  - Logistic regression models
  - Separate model building for pre and post variables

# Final pretest and posttest models

All else held constant, the more somebody values statistics and its usefulness (i.e., the higher their pretest *Value* score) going into the pretest, the lower their expected pretest achievement.

|   | Dependent variable:       |                         |  |
|---|---------------------------|-------------------------|--|
|   | Correct LOCUS Pre<br>Item | Correct LOCUS Post Item |  |
|   | (1)                       | (2)                     |  |
| onstant   | 0.084                     | -0.966                  |  |
|   | (0.011, 0.157)            | (-1.225, -0.707)        |  |
|   | p=0.025**                 | p = 0.000***            |  |
| entered <i>Cognitive Competence</i> (at e time) | -0.123                    | -0.164                  |  |
|   | (-0.234, -0.012)          | (-0.272, -0.057)        |  |
|   | p = 0.030**               | p = 0.004***            |  |
| entered Value (at the time)                     | -0.227                    | 0.053                   |  |
|   | (-0.349, -0.105)          | (-0.109, 0.215)         |  |
|   | p = 0.0004***             | p = 0.523               |  |
| Iale indicator                                  | 0.150                     | 0.020                   |  |
|   | (0.010, 0.290)            | (-0.129, 0.168)         |  |
|   | p=0.037**                 | p = 0.796               |  |
| alue/Male interaction term                      |                           | -0.309                  |  |
|   |                           | (-0.592, -0.025)        |  |
|   |                           | p=0.034**               |  |
| ognitive Competence/Male<br>teraction term      | -0.258                    |                         |  |
|   | (-0.471, -0.045)          |                         |  |
|   | $p = 0.019^{**}$          |                         |  |
| otal number of correct items in the retest      |                           | 0.110                   |  |
|   |                           | (0.090, 0.131)          |  |
|   |                           | $p = 0.000^{***}$       |  |
| Residual Deviance                               | 629.971 (df = 323)        | 492.227 (df = 285)      |  |
| ull Deviance                                    | 711.011 (df = 327)        | 770.931 (df = 290)      |  |

All else held constant, the more a female student values statistics in the posttest, the higher their expected posttest achievement. For male students, it remains a **decrease** (in expected posttest achievement).

Cls have a confidence level of 95%.

Tables created with Hlavac's stargazer R package (2018)

### Conclusion

- The LOCUS's proposed four-construct structure was not recovered in our EFA and that raises concerns (more work is needed)
- We were able to find empirical evidence of relationships between certain attitude scale scores (on the SATS) and achievement (on the LOCUS)
- How one administers the assessment may affect responses
  - Additional data is needed to address whether counting the LOCUS for participation or a grade matters (and, if so, which should be recommended)
  - Low-quality LOCUS attempts discovered while modelling are suggestive that test administration decisions may have an effect

### Limitations and Future Directions

- We relied heavily on pairwise-complete or complete data throughout the project, and in doing so, may have dropped crucial data
  - A formal investigation into the types of missingness in this data would be appropriate
- More sophisticated models for the internal structure of the LOCUS should be used in future work
  - Confirmatory Factor Analysis
  - Item Response Theory

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## Supplementary Slides

Table of loadings for four-factor solution of pretest with varimax rotation

|         | Factor 1 | Factor 2 | Factor 3 | Factor 4 | Communality | Nominal Construct   |
|---------|----------|----------|----------|----------|-------------|---------------------|
| Item 2  | 0.2879   | 0.5325   | 0.3783   | -0.2345  | 0.5645      | Formulate Questions |
| Item 5  | 0.2699   | 0.1139   | 0.2877   | -0.0575  | 0.1719      | Formulate Questions |
| Item 9  | 0.3603   | 0.2150   | 0.0939   | 0.0843   | 0.1920      | Formulate Questions |
| Item 12 | 0.3281   | 0.2543   | 0.0552   | 0.0054   | 0.1754      | Formulate Questions |
| Item 3  | 0.2632   | 0.2484   | 0.4215   | 0.0019   | 0.3086      | Collect Data        |
| Item 6  | 0.3548   | 0.1611   | 0.1450   | 0.1544   | 0.1967      | Collect Data        |
| Item 10 | 0.3289   | 0.1520   | 0.1284   | 0.0680   | 0.1524      | Collect Data        |
| Item 13 | 0.5523   | 0.1270   | 0.0688   | -0.0888  | 0.3338      | Collect Data        |
| Item 21 | 0.2354   | 0.0290   | -0.0392  | 0.0014   | 0.0578      | Collect Data        |
| Item 7  | 0.2775   | 0.2173   | 0.2261   | 0.0265   | 0.1760      | Analyze Data        |
| Item 11 | 0.2356   | 0.1707   | 0.1313   | 0.3647   | 0.2349      | Analyze Data        |
| Item 15 | 0.2478   | 0.0577   | 0.0725   | 0.0958   | 0.0792      | Analyze Data        |
| Item 16 | 0.0184   | 0.2069   | 0.3575   | 0.0550   | 0.1740      | Analyze Data        |
| Item 18 | 0.0863   | -0.0095  | 0.0819   | 0.4863   | 0.2508      | Analyze Data        |
| Item 20 | 0.1363   | 0.0120   | 0.4448   | 0.3098   | 0.3125      | Analyze Data        |
| Item 1  | 0.3394   | 0.6365   | 0.1205   | 0.0424   | 0.5366      | Interpret Results   |
| Item 4  | 0.3569   | 0.3616   | 0.0231   | 0.2790   | 0.3365      | Interpret Results   |
| Item 8  | 0.2436   | 0.4343   | 0.2013   | 0.2332   | 0.3428      | Interpret Results   |
| Item 14 | 0.0439   | -0.0121  | 0.0542   | 0.3267   | 0.1117      | Interpret Results   |
| Item 17 | -0.0118  | 0.0804   | -0.2742  | 0.3753   | 0.2227      | Interpret Results   |
| Item 19 | -0.0448  | 0.1580   | 0.1176   | 0.2428   | 0.0998      | Interpret Results   |
| Item 22 | 0.7005   | -0.0157  | 0.3412   | -0.0764  | 0.6132      | Interpret Results   |
| Item 23 | -0.0326  | -0.0089  | -0.0528  | 0.1036   | 0.0147      | Interpret Results   |

We considered an item as loaded onto (or sufficiently associated with) a factor if the absolute value of its loading on that factor was greater than 0.4, as suggested by Swisher et al. (2004). If an item loads onto a factor, it is highlighted under that factor.

### Proportion

of Variance 0.0902 0.0615 0.0492 0.0451 Explained

Cumulative Variance 0.0902 0.1517 0.2009 0.2460 Explained

### Table of loadings for two-factor solution of pretest with varimax rotation

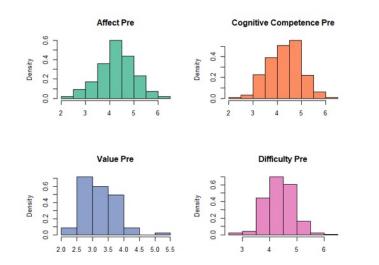
|         | Factor 1 | Factor 2 | Communality | Nominal Construct   |
|---------|----------|----------|-------------|---------------------|
| Item 2  | 0.6506   | -0.1638  | 0.4502      | Formulate Questions |
| Item 5  | 0.3947   | -0.0692  | 0.1606      | Formulate Questions |
| Item 9  | 0.4137   | 0.1026   | 0.1817      | Formulate Questions |
| Item 12 | 0.3940   | 0.0359   | 0.1565      | Formulate Questions |
| Item 3  | 0.5147   | 0.0028   | 0.2649      | Collect Data        |
| Item 6  | 0.4018   | 0.1675   | 0.1895      | Collect Data        |
| Item 10 | 0.3761   | 0.0757   | 0.1472      | Collect Data        |
| Item 13 | 0.4898   | -0.0691  | 0.2447      | Collect Data        |
| Item 21 | 0.1634   | 0.0146   | 0.0269      | Collect Data        |
| Item 7  | 0.4211   | 0.0392   | 0.1789      | Analyze Data        |
| Item 11 | 0.3045   | 0.3860   | 0.2417      | Analyze Data        |
| Item 15 | 0.2388   | 0.0982   | 0.0667      | Analyze Data        |
| Item 16 | 0.2805   | 0.0571   | 0.0819      | Analyze Data        |
| Item 18 | 0.0750   | 0.4686   | 0.2252      | Analyze Data        |
| Item 20 | 0.2946   | 0.2422   | 0.1455      | Analyze Data        |
| Item 1  | 0.6052   | 0.1171   | 0.3800      | Interpret Results   |
| Item 4  | 0.4428   | 0.3134   | 0.2943      | Interpret Results   |
| Item 8  | 0.4830   | 0.2740   | 0.3083      | Interpret Results   |
| Item 14 | 0.0360   | 0.3245   | 0.1066      | Interpret Results   |
| Item 17 | -0.1084  | 0.3847   | 0.1597      | Interpret Results   |
| Item 19 | 0.0945   | 0.2510   | 0.0719      | Interpret Results   |
| Item 22 | 0.6207   | -0.0684  | 0.3900      | Interpret Results   |
| Item 23 | -0.0591  | 0.1106   | 0.0157      | Interpret Results   |

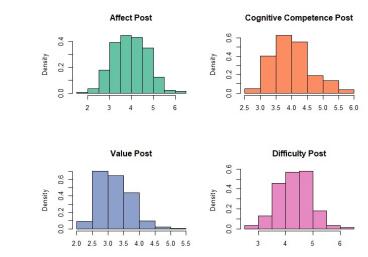
| Proportion of       | 0.1498 | 0.0454 |  |
|---------------------|--------|--------|--|
| Variance Explained  | 0.1498 | 0.0434 |  |
| Cumulative Variance | 0.1498 | 0.1952 |  |
| Explained           | 0.1498 | 0.1932 |  |

We considered an item as loaded onto (or sufficiently associated with) a factor if the absolute value of its loading on that factor was greater than 0.4, as suggested by Swisher et al. (2004). If an item loads onto a factor, it is highlighted under that factor.

### Predictors we were interested in

- For the pretest models: the (centered) pretest SATS-28 scale scores
- For the posttest models: the (centered) posttest SATS-28 scale scores *and* the number of correct items in the pretest
- We also included section and gender as covariates in the model-building process (via indicator variables)
  - Including section as a predictor allowed us try and account, at least a little, for section-to-section differences





### Sample LOCUS Formulate Questions Item

### Question 2 of 23

### Time left: 01:06:37

Thirty balloons were selected at random from a box of 60 balloons and filled with helium. The other 30 balloons were filled with regular air. The circumference of each balloon was measured immediately after being filled and then again three days later. Based on the data, which of the following questions could be answered?

### Choose one

- O Are helium-filled balloons more popular than air-filled balloons are?
- O Do helium-filled balloons float higher after three days than air-filled balloons do?
- O Do helium-filled balloons shrink more in three days than air-filled balloons do?
- O Is it easier to fill balloons with helium than to fill them with air?

### Back

Next

### Sample LOCUS Collect Data Item

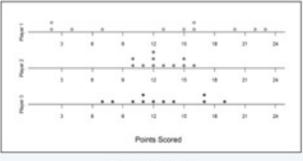
| ne le | ft: 01:05:09  |
|-------|---|
| uld   | ts are interested in knowing about support for an effort to recycle glass products. Which one of the following ways<br>they use to select a sample of adults from 100 households in their town?<br>SE ONE |
|       |   |
| 0     | Ask 25 adults at each of the 4 grocery stores located in different parts of the town.   |
| 0     | Ask 1 adult from each of 100 households randomly selected from the town's household list.   |
| 0     | Divide the town into 20 areas, and in each area ask 1 adult from each of the first 5 households that have someone at home.  |
| 0     | Randomly select 100 students at the school who then each ask 1 adult in their own household.  |
| ack   |   |

### Sample LOCUS Analyze Data Item

### Question 4 of 23

### Time left: 01:05:54

Jason is the statistician for a summer basketball league. After eleven games he notes that the top three scorers in the league have about the same mean number of points per game (12.7, 12.7, and 12.6). He produces the dotplots of the points scored in eleven games for each player shown below.



Click image to enlarge.

Which of the following best describes the additional information, if any, provided by the dotplots about the players' performances?

### er Choose one

0

Player 1's scores have a smaller median and are more variable than the others.
Player 1 always scores more points per game than either of the other two players.
Player 2's scores are least variable, and Player 1's scores are most variable.

The dotplots do not provide any additional information.

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### Sample LOCUS Interpret Results Item

### Question 7 of 23

### Time left: 01:04:47

The table below summarizes data from a survey of 1,000 adults. Each respondent was asked whether he or she was a high school graduate and whether he or she had an annual income of more than \$40,000 per year.

| ANNUAL INCOME      | HIGH SCHOOL GRADUATE | NOT A HIGH SCHOOL GRADUATE | TOTAL |
|--------------------|----------------------|----------------------------|-------|
| \$40,000 or less   | 250                  | 150                        | 400   |
| More than \$40,000 | 500                  | 100                        | 600   |
| Total              | 750                  | 250                        | 1000  |

Which of the following provides the best justification for an association between a person's income and whether he or she is a high school graduate?

### Choose one

| 0 | About 67% (500/750) of the high school graduates have an annual income of more than \$40,000 compared to only 40% (100/250) of the non-high school graduates.   |
|---|---|
| 0 | 75% (750/1000) of the respondents graduated from high school, and 60% (600/1000) of the respondents have an annual income of more than \$40,000.                |
| 0 | There are 500 high school graduates with annual incomes of more than \$40,000 but only 250 high school graduates<br>with annual incomes of \$40,000 or less.    |
| 0 | There are 500 high school graduates with annual incomes of more than \$40,000 but only 100 non-high school graduates with annual incomes of more than \$40,000. |
| _ |   |